

Homework #2

Due 2/27

Problems

3.2

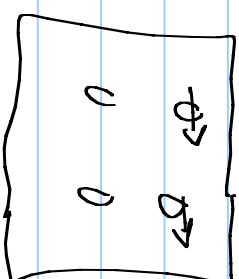
3.12

3.30

} compute A_n

\rightarrow compute ϕ_{P_n} (same as ϕ_{R_n})

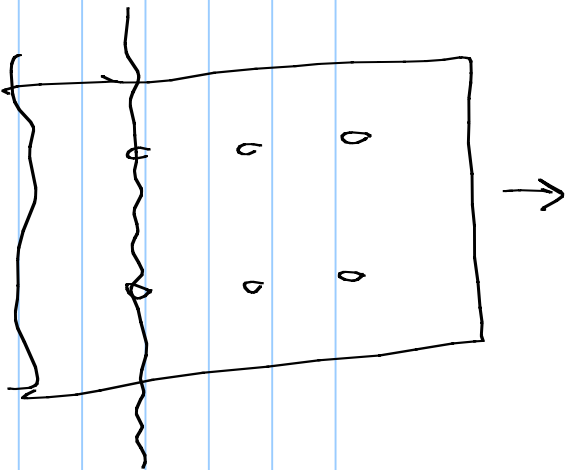
$W = 1 - x/q$



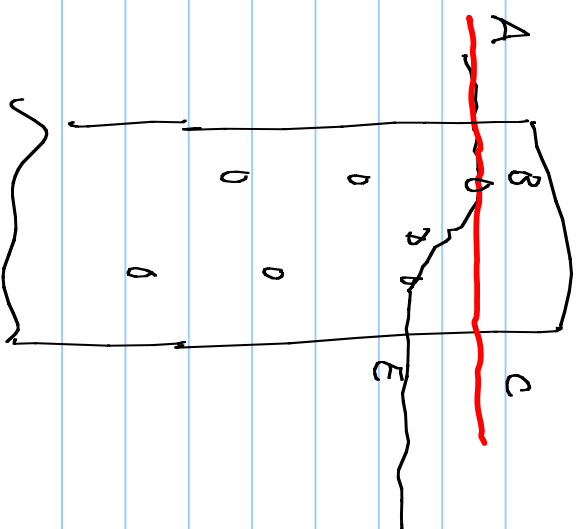
Review: Two Limit States

Yielding
Fracture

T



Staggered Bolts



- Gives a larger net area
- Might be used for odd # of bolts

Two possible fracture planes

A - B - C

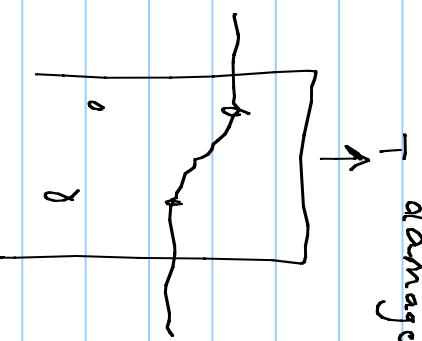
A - B - D - E

Fracture plane w/ smallest net area is the controlling case

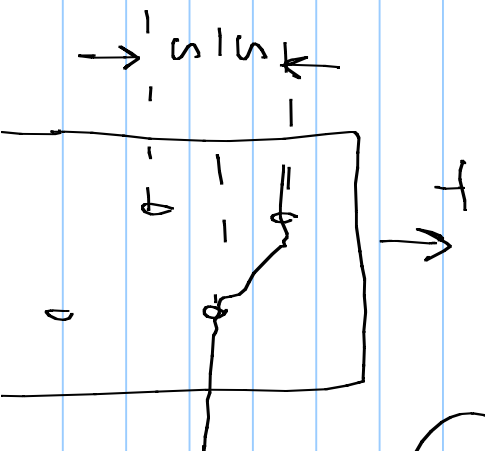
Without stagger : $A_n = A_g - \sum d_i \left(\text{bolt diameter} + \frac{1}{16} + \frac{1}{16} \right) (t)$

With Stagger : Need to account for :

1. Different # of holes
2. Longer fracture plane
3. Stress along incline is not pure tension



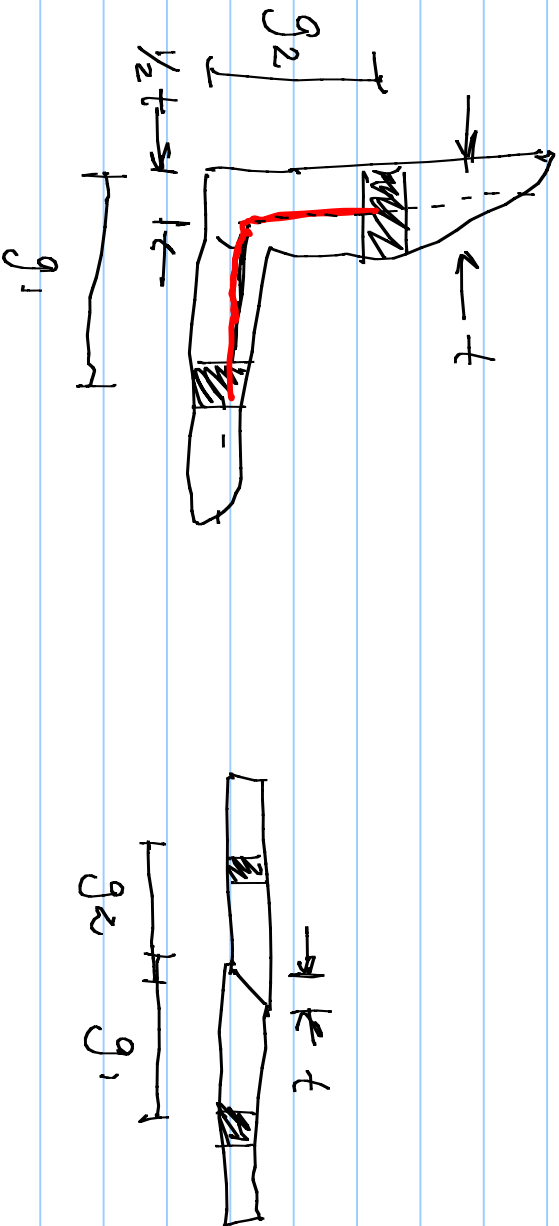
Use empirical to predict tension capacity change



$S = \text{pitch}$
 $g = \text{gage distance}$

H
g

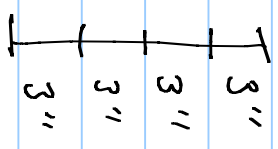
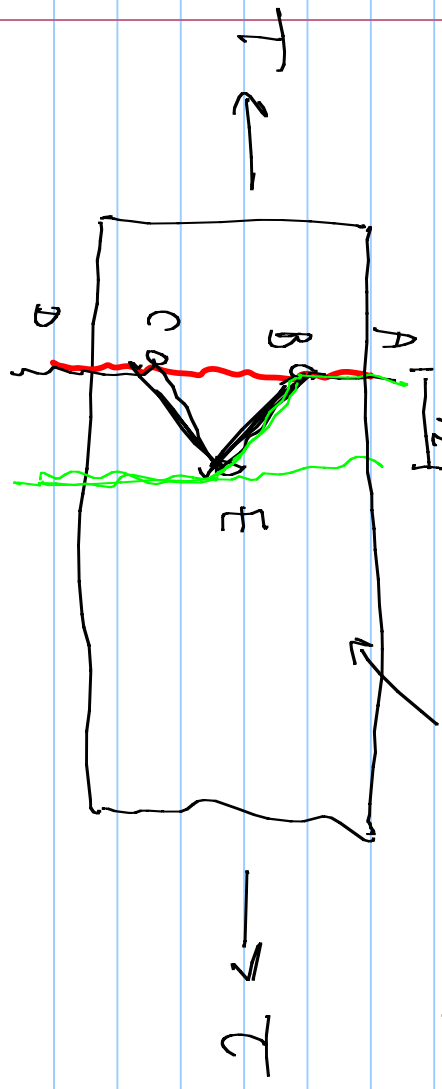
$$A_n = A_g - \left[\sum (\text{bolt diameter} + \frac{1}{16} + \frac{1}{16}) (t) + \left(\sum \frac{S^2}{4g} \right) (t) \right]$$



$$g = g_1 - \frac{1}{2}t + g_2 - \frac{1}{2}t = g_1 + g_2 - t$$

Problem 3-10

PL 12 x 3/4



Find Net Area. $\frac{3}{4}$ " ϕ bolts

Check : A-B-C-D

A-B-E-C-D

From inspection : E (1 bolt > 2 bolts)
 A-B-E (2 bolts + stagger > 2 bolts w/o stagger)

$$ABCD : A_n = A_g - 2 \left(\frac{3}{4} + \frac{1}{8} \right) \left(\frac{3}{4} \right)$$

$$A_n = (12) \left(\frac{3}{4} \right) - 2 \left(\frac{7}{8} \right) \left(\frac{3}{4} \right)$$

$$A_n = 9 -$$

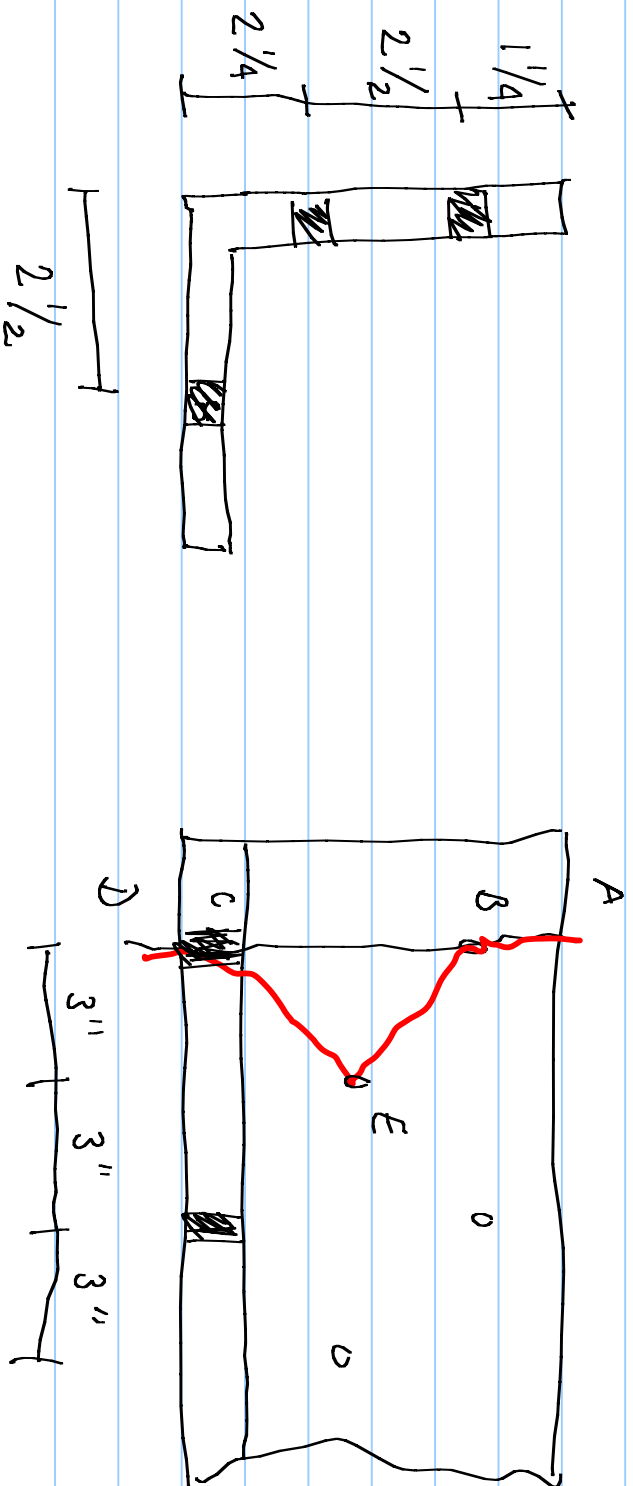
$$A_n = 7.69 \text{ in}^2$$

$$ABECD : A_n = A_g - 3 \left(\frac{3}{4} + \frac{1}{8} \right) \left(\frac{3}{4} \right) + \sum \frac{S^2}{4g} (t)$$

$$A_n = 12 \left(\frac{3}{4} \right) - 3 \left(\frac{7}{8} \right) \left(\frac{3}{4} \right) + \frac{(2)}{4} \frac{1.5^2}{(3)} \left(\frac{3}{4} \right)$$

$$A_n = 7.31 \text{ in}^2$$

Example 2: $L 6 \times 4 \times \frac{1}{2}$, $\frac{7}{8}$ " diameter - 60 lbs



- A - B - C - D
- A - B - E - C - D

$$A_g = 4.75 \text{ in}^2$$

w/out Stagger, A-B-C-D : $A_n = 4.75 - 2 \left(\frac{7}{8} + \frac{1}{8} \right) \left(\frac{1}{2} \right)$

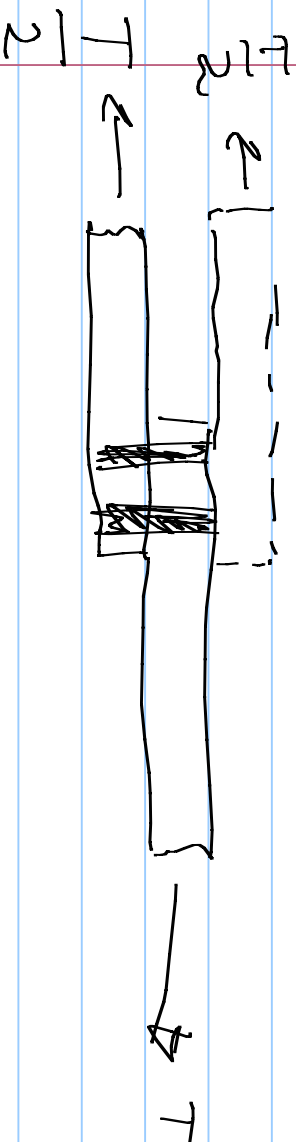
$$A_n = 3.75 \text{ in}^2$$

w/s stagger : A-B-E-C-D : $A_n = 4.75 - 3 \left(\frac{7}{8} + \frac{1}{8} \right) \left(\frac{1}{2} \right) +$

$$\left[\frac{3^2}{4(2.5)} + \frac{3^2}{4(4.25)} \right] \left[\frac{1}{2} \right]$$
$$2 \frac{1}{4} + 2 \frac{1}{2} - \frac{1}{2}$$

$$A_n = 3.96 \text{ in}^2$$

"Symmetry"



Design of Tension Members

$$\phi R_n \leq \phi R_n = f(\phi, F, \textcircled{A})$$

Tension member design dictated by area.

A_g → yielding
 A_n }
 A_e } → fracture

1. Required Area, Yielding

$$\phi R_n = 0.9 F_y A_g \geq P_u$$

$$A_g \geq \frac{P_u}{0.9 F_y}$$

2. Required Area, Fracture

$$\phi R_n = 0.75 F_u A_e \geq P_u$$

$$0.75 F_u U A_n \geq P_u$$

\downarrow
estimate for initial design

$$0.75 F_u U (A_g - A_{5k}) \geq P_u$$

$$A_g \approx \frac{P_u}{0.75U F_u} + A_{bh}$$

↙ estimate ↘