

Summary of Discrete Compounding Formulas with Discrete Payments

Flow Type	Factor Notation	Formula	Cash Flow Diagram	Factor Relationship
SINGLE	Compound amount (F/P, i, N)	$F = P(1 + i)^N$		$(F/P, i, N) = (F/A, i, N) + 1$
	Present worth (P/F, i, N)	$P = F(1 + i)^{-N}$		$(P/F, i, N) = 1 - (P/A, i, N)i$
EQUALLY PAYMENT	Compound amount (F/A, i, N)	$F = A \left[\frac{(1 + i)^N - 1}{i} \right]$		$(A/F, i, N) = (A/P, i, N) - i$
	Sinking fund (A/F, i, N)	$A = F \left[\frac{i}{(1 + i)^N - 1} \right]$		$(A/P, i, N) = \frac{i}{1 - (P/F, i, N)}$
PRESENT SERIES	Present worth (P/A, i, N)	$P = A \left[\frac{(1 + i)^N - 1}{i(1 + i)^N} \right]$		$(A/P, i, N) = \frac{i}{1 - (P/F, i, N)}$
	Capital recovery (A/P, i, N)	$A = P \left[\frac{i(1 + i)^N}{(1 + i)^N - 1} \right]$		
GRADIENT SERIES	Linear gradient Present worth (P/G, i, N)	$P = G \left[\frac{(1 + i)^N - iN - 1}{i^2(1 + i)^N} \right]$		$(F/G, i, N) = (P/G, i, N) (F/P, i, N)$ $(A/G, i, N) = (P/G, i, N) (A/P, i, N)$
	Geometric gradient Present worth (P/A ₁ , g, i, N)	$P = \begin{cases} A_1 \left[\frac{1 - (1 + g)^N (1 + i)^{-N}}{i - g} \right] \\ \frac{NA_1}{1 + i} \quad (\text{if } i = g) \end{cases}$		$(F/A_1, g, i, N) = (P/A_1, g, i, N) (F/P, i, N)$